#### Suspect Research & Statistical Inferences

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### Suspect research practices

- Suspect practices *can* lead to inaccurate findings (e.g., Hedges, 2017; Lindsay, 2012).
- How much? Depends on which suspect practice...
- Conditional data collection: failing significance, get more data!?
  - 1. Bias treatment effect estimates
  - 2. Bias can be large ( $\sim 50\%$ )
  - 3. Bias can arise even if no analyses are conducted

### Conditional data collection

- John, Loewenstein, & Prelec (2012): >50% of respondents admitted they had collected more data based on a nonsignificant result.
- Fiedler & Schwartz (2016): >30% of respondents admitted to collecting more data in order to render a nonsignificant result significant.
- Simmons, Nelson, & Simonsohn (2011): Inflated type I error rates (~10-20%)
- Related to sequential trials in medicine (Nardini & Sprenger, 2012)

## Conditional data collection

- Treatment effect  $\theta \neq 0$
- Initial experiment (n subjects in each of treatment & control)
  - Estimate T<sub>0</sub> (mean difference)
- Concomitant variable O correlated with  $T_0$
- Based on O either:
  - 1. Report  $T_0$
  - 2. Continue experiment
    - Recruit more subjects (*m* subjects per arm)
    - ► Report *T*<sub>1</sub>

### Conditional inferences

- We only observe an estimate conditional on O:
  - 1.  $T_0|O$ 2.  $T_1|O$
- Bias:

1. 
$$E[T_0|O] - \theta$$
  
2.  $E[T_1|O] = \frac{n}{m+n} (E[T_0|O] - \theta)$ 

• If *O* is correlated to *T*<sub>0</sub>, the treatment effect can be biased.

- 1. Data are normally distributed, with known variance.
- 2. n subjects per arm in initial experiment

• 
$$T_0 \sim N(\theta, 2\sigma^2/n)$$

3. *m* subjects added per arm, whose responses are independent of past observations.

# Conditional on significance

- $O = \mathbf{1}\{|T_0| > 1.96\sqrt{2\sigma^2/n}\}; (\alpha = .05, 2\text{-tailed test})$  Stop if O = 1, continue if O = 0
- T<sub>0</sub> will be a truncated normal



## Collecting data based on nonsignificance



### Other concomitant variables

- "If O is correlated to T<sub>0</sub>, the treatment effect can be biased."
  Me, three slides ago.
- Researchers may observe any number of variables correlated with  $T_0$ .
  - Casual observations may be correlated with  $T_0$ .
  - If more data are collected based on them,  $T_1|O$  can be biased.
  - No analysis of intial data needed.
- How might these variables convey information about  $T_0$ ?
  - How likely is it that  $\mathcal{T}_0$  will be significant given what was observed?

## Information about possible significance

- Probabilistic model
- O provides information about how likely  $T_0$  is to be significant:
  - $P[T_0 \text{ significant}|O] = \eta$
- For a given probability of significance  $(\eta)$ , a researcher may
  - stop and report  $T_0|\eta$
  - collect more data and report  $T_1|\eta$
- Assume *O* conveys *only* information about the probability of significance.
  - $T_0|O$  has a reweighted normal distribution

### Continuing due to improbable significance



#### Unknowable bias

- It may be impossible to determine exactly what information any observation conveys about  $T_0$ .
- If it carries *any* information, and the decision to collect more data depends on it, we know that  $T_1$  can be biased.
- We may have no idea how biased a given result is.
- Ad-hoc data collection can bias a treatment effect estimate even if no analysis of interim data is conducted. It may be impossible to know how much this bias is!

## Conclusions

- Bias from conditionally collected data can be substantial, even if a researcher does not actually run a significance test.
- Pre-registration can improve transparency, and help curtail more passive forms of CDC.
  - SREE!
- Blinding?
- Empirical replication of past results.

#### References

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Thank You!

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# Stopping for significance



#### Repeated waves



#### Percent Bias of $T_k | T_{k-1}$ Not Significant

#### Repeated waves, reporting only significant results



# Distributions: probable significance



# Stopping for probable significance

